

Circle Theorems

Angles at Centre & Circumference / Angle in a Semicircle / Theorems with Chords & Tangents / Angles in Cyclic Quadrilaterals / Angles in the Same Segment / The Alternate Segment Theorem / Circle Theorem Proofs

Medium (17 questions)	/59
Hard (13 questions)	/52
Very Hard (16 questions)	/74
Total Marks	/185

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Medium Questions

1

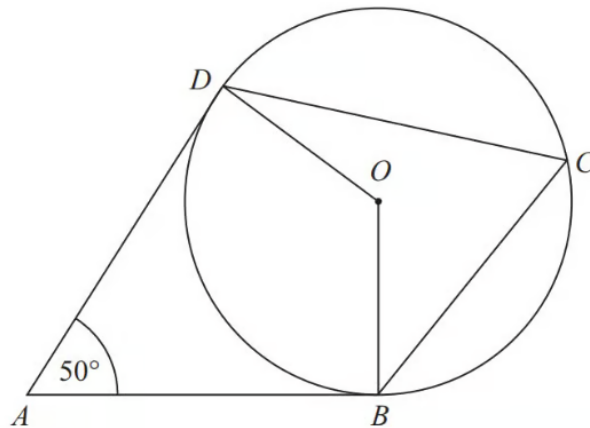


Diagram **NOT**
accurately drawn

B , C and D are points on the circumference of a circle, centre O . AB and AD are tangents to the circle.

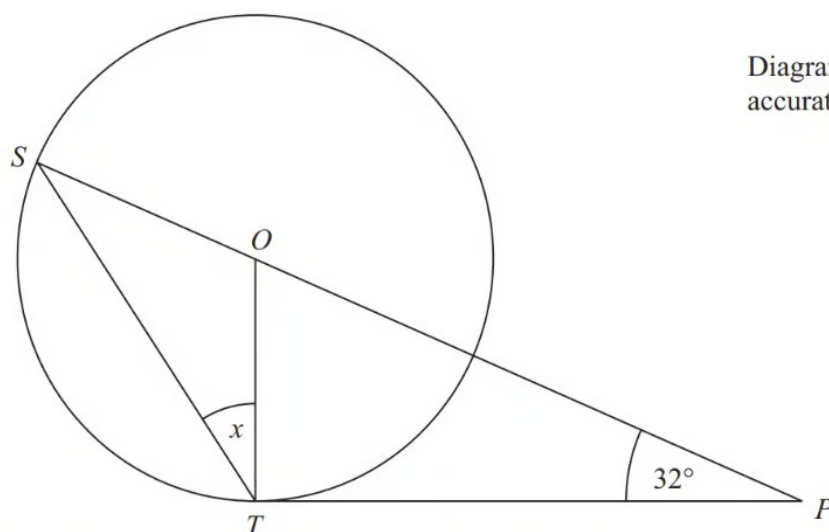
Angle $DAB = 50^\circ$

Work out the size of angle BCD .

Give a reason for each stage in your working.

(4 marks)

Diagram **NOT**
accurately drawn



S and T are points on the circumference of a circle, centre O .

PT is a tangent to the circle.

SOP is a straight line.

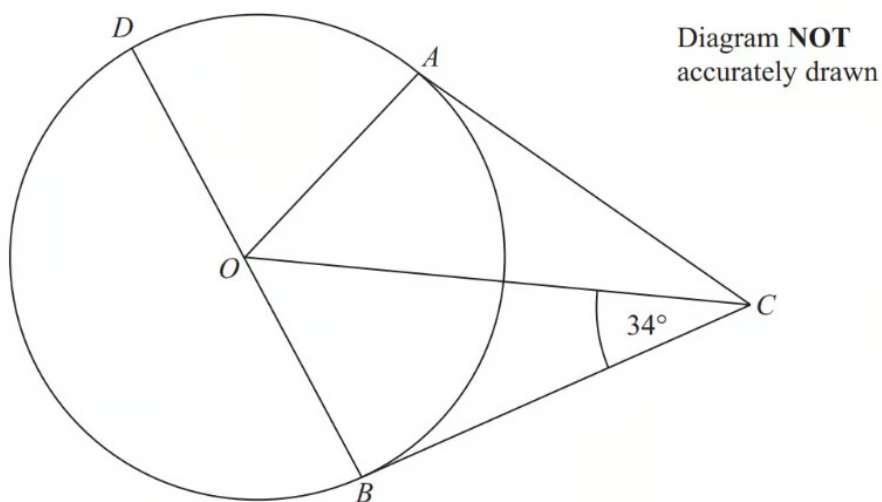
Angle $OPT = 32^\circ$

Work out the size of the angle marked x .

Give reasons for your answer.

(5 marks)

3



A , B and D are points on the circumference of a circle, centre O . BOD is a diameter of the circle.

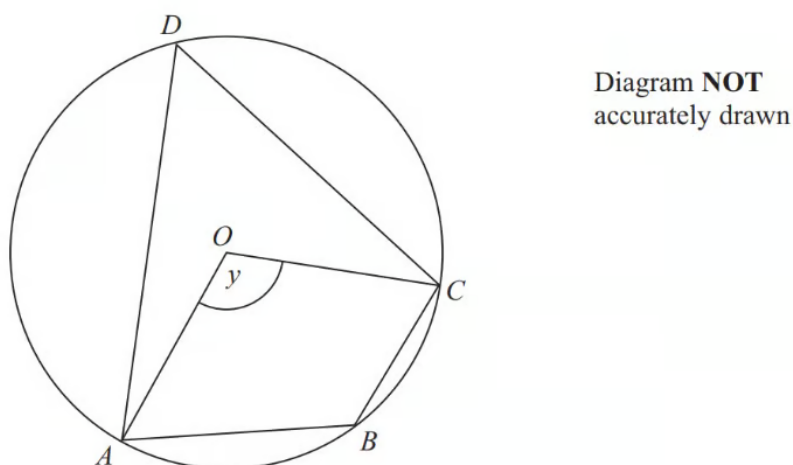
BC and AC are tangents to the circle.

Angle $OCB = 34^\circ$.

Work out the size of angle DOA .

(3 marks)

4



A , B , C and D are points on the circumference of a circle, centre O .

Angle $AOC = y$.

Find the size of angle ABC in terms of y .

Give a reason for each stage of your working.

(4 marks)

5

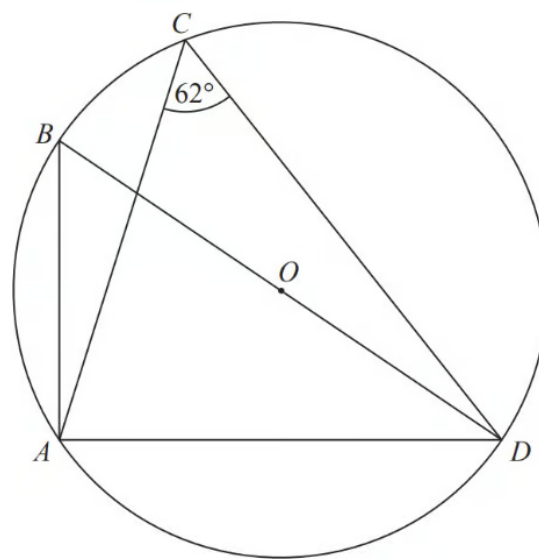


Diagram **NOT**
accurately drawn

A , B , C and D are points on the circumference of a circle, centre O .

BOD is a straight line.

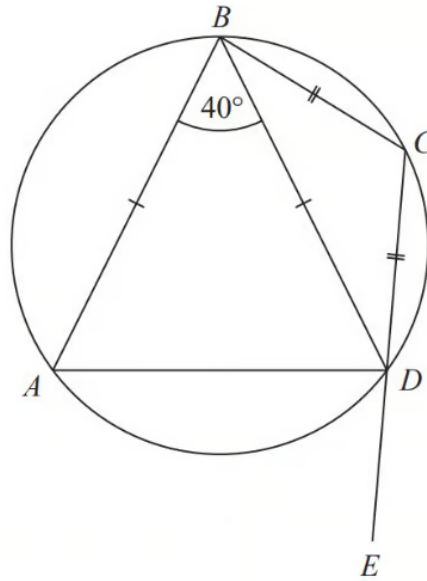
Angle $ACD = 62^\circ$

Find the size of angle ADB .

Give a reason for each stage in your working.

(4 marks)

- 6 The points A , B , C and D lie on a circle.
 CDE is a straight line.



$$BA = BD$$

$$CB = CD$$

$$\text{Angle } ABD = 40^\circ$$

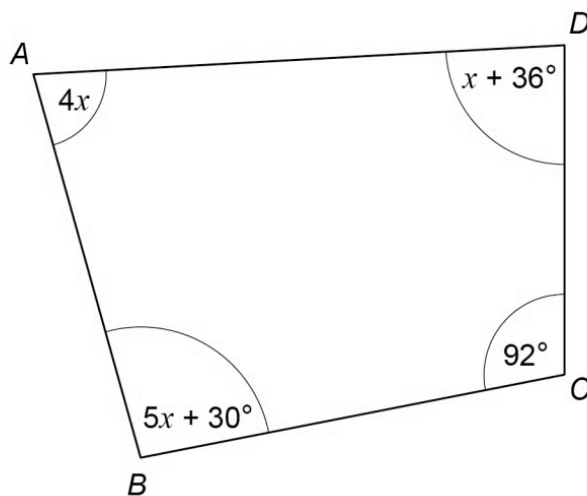
Work out the size of angle ADE .

You must give a reason for each stage of your working.

(5 marks)

7 $ABCD$ is a quadrilateral.

Not drawn
accurately

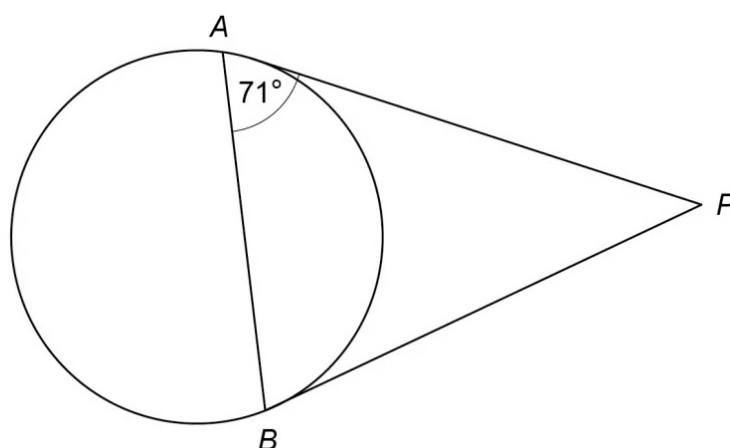


Prove that $ABCD$ is **not** a cyclic quadrilateral.

(4 marks)

8 A and B are points on a circle.

PA and PB are tangents.



Not drawn
accurately

Work out the size of angle APB .

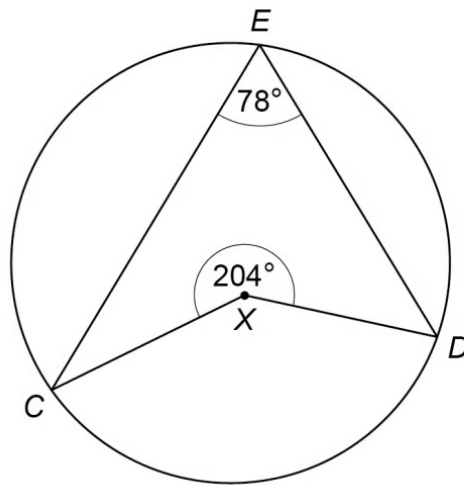
.....degrees

(2 marks)

9 C , D and E are points on a circle.

$$XC = XD.$$

Not drawn
accurately



Is X the centre of the circle?

Tick a box.

☐ Yes

☐ No

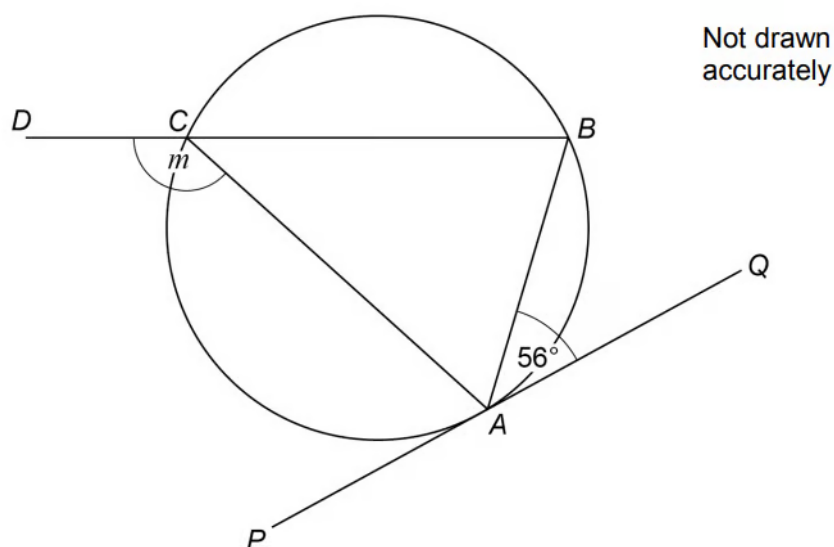
Show working to support your answer.

(2 marks)

10 A , B and C are points on a circle.

DCB is a straight line.

PAQ is a tangent to the circle.



Sam is trying to work out the size of angle m . Here is his working.

$\text{angle } ACB = 56^\circ$	angles in the same segment are equal
$m = 180^\circ - 56^\circ$	angles at a point on a straight line add up to 180°
$m = 124^\circ$	

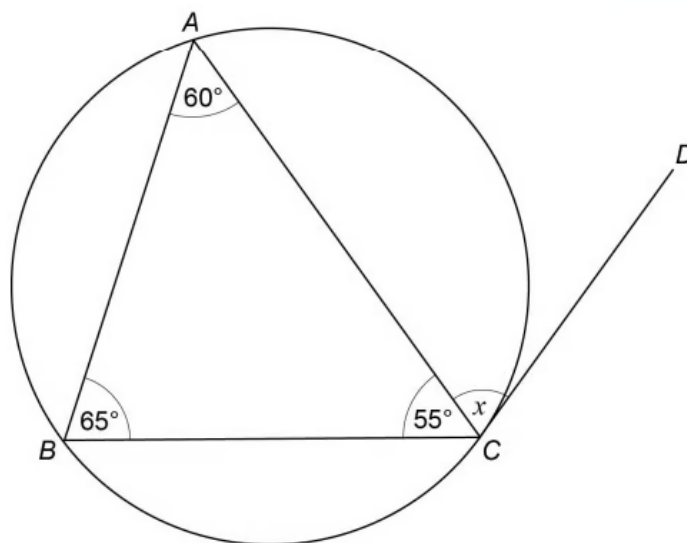
Make a criticism of his working.

(1 mark)

11 A , B and C are points on a circle.

CD is a tangent to the circle.

Not drawn
accurately

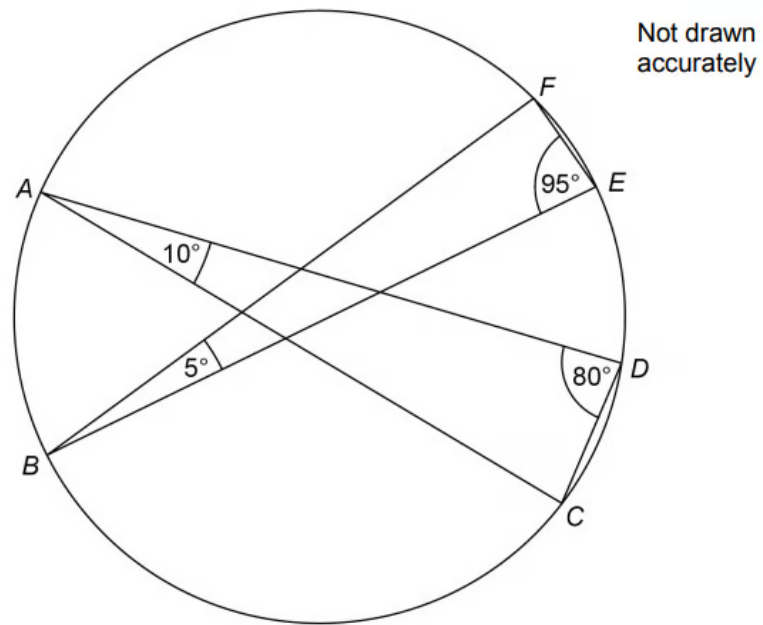


Write down the size of angle x .
Give a reason for your answer.

.....degrees

(2 marks)

12 A, B, C, D, E and F are points on a circle.



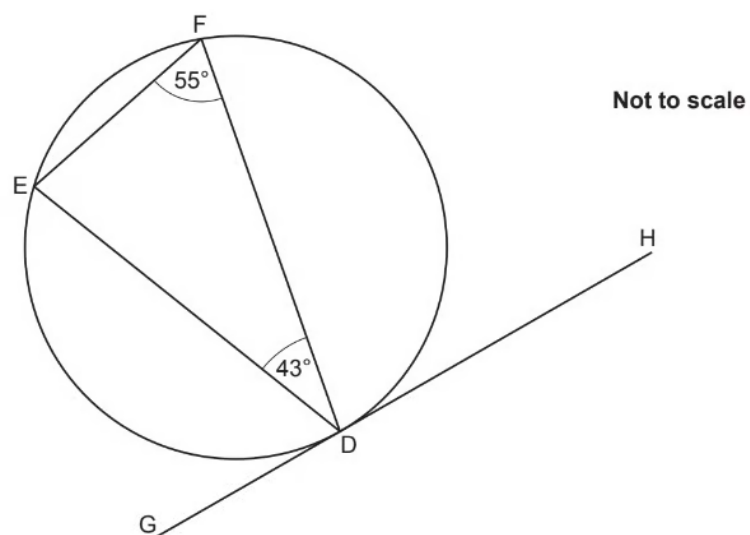
Choose the line that is a diameter of the circle.

- A. BE
- B. AD
- C. AC
- D. BF

(2 marks)

13 In the diagram,

- E, F and D are points on the circumference of the circle
- G, D and H lie on a tangent to the circle
- angle $EFD = 55^\circ$
- angle $FDE = 43^\circ$.

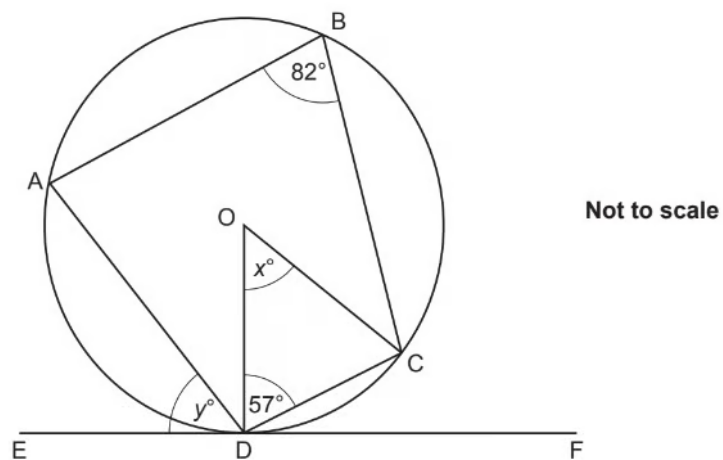


Explain why angle HDF is 82° .

(4 marks)

14 (a) The diagram shows a circle, centre O.

Points A, B, C and D lie on the circumference of the circle.
 EDF is a tangent to the circle.
 Angle $ABC = 82^\circ$ and angle $ODC = 57^\circ$.



Work out the value of x .

$x = \dots\dots\dots$

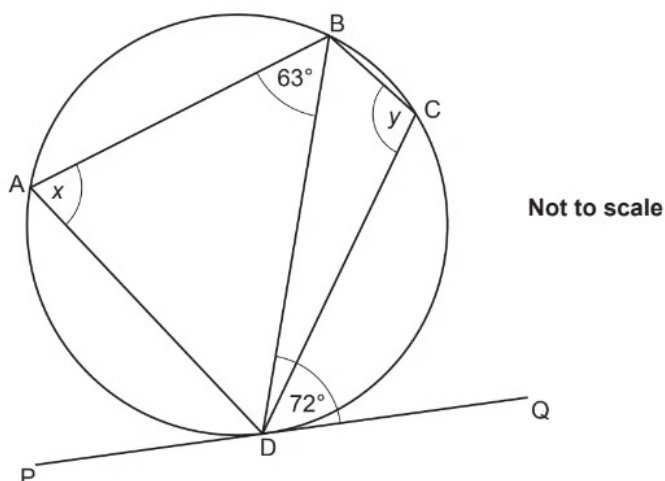
(2 marks)

(b) Work out the value of y .

$y = \dots\dots\dots$

(3 marks)

15 (a) A, B, C and D are points on the circumference of a circle.



PQ is a tangent to the circle at D.
Angle $BDQ = 72^\circ$ and angle $ABD = 63^\circ$.

Work out angle x .
Give a reason for your answer.

Angle $x = \dots\dots\dots^\circ$ because $\dots\dots\dots$

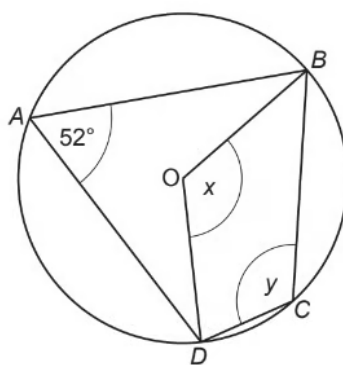
(2 marks)

(b) Work out angle y .
Give a reason for your answer.

Angle $y = \dots\dots\dots^\circ$ because $\dots\dots\dots$

(2 marks)

16 (a) A, B, C and D are points on the circumference of a circle, centre O.



Not to scale

Angle BAD = 52° .

Work out angle x .

Give a reason for your answer.

$x = \dots\dots\dots^\circ$ reason $\dots\dots\dots$

(2 marks)

(b) Work out angle y .

Give a reason for your answer.

$y = \dots\dots\dots^\circ$ reason $\dots\dots\dots$

(2 marks)

17 D, E, F and G are points on a circle, centre O

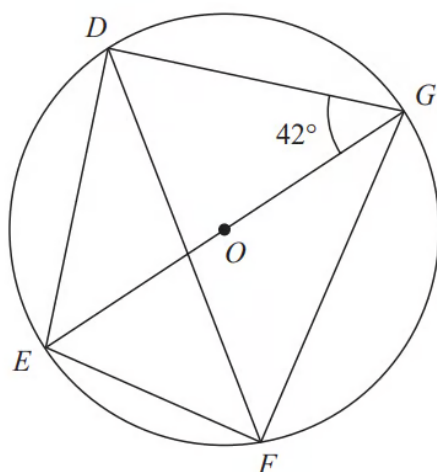


Diagram **NOT**
accurately drawn

EOG is a diameter of the circle.

Angle $EGD = 42^\circ$

Calculate the size of angle DFG

Give a reason for each stage of your working.

Angle $DFG = \dots\dots\dots$

(4 marks)

Hard Questions

1

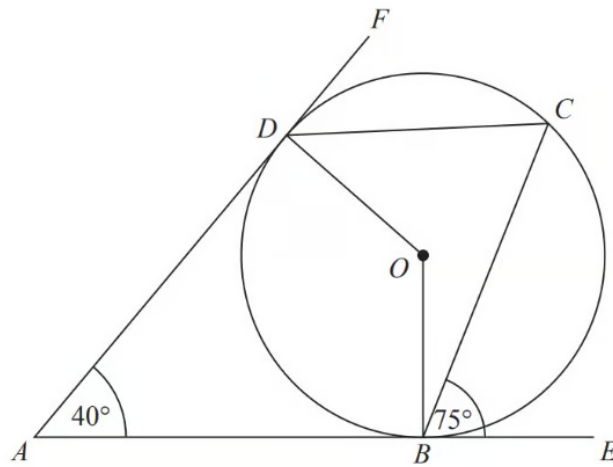


Diagram **NOT**
accurately drawn

B , C and D are points on the circumference of a circle, centre O . ABE and ADF are tangents to the circle.

Angle $DAB = 40^\circ$

Angle $CBE = 75^\circ$

Work out the size of angle ODC .

(3 marks)

2

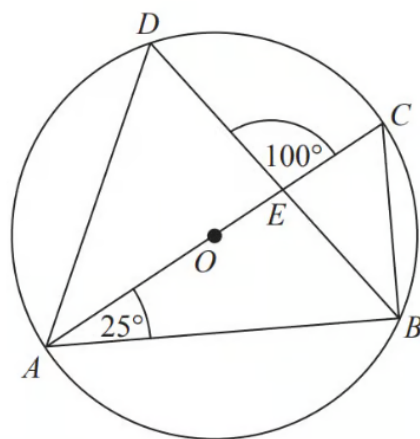


Diagram **NOT**
accurately drawn

A , B , C and D are points on the circumference of a circle, centre O .
 AC is a diameter of the circle.
 AC and BD intersect at E .

Angle $CAB = 25^\circ$
 Angle $DEC = 100^\circ$

Work out the size of angle DAC .
 You must show all your working.

(4 marks)

3

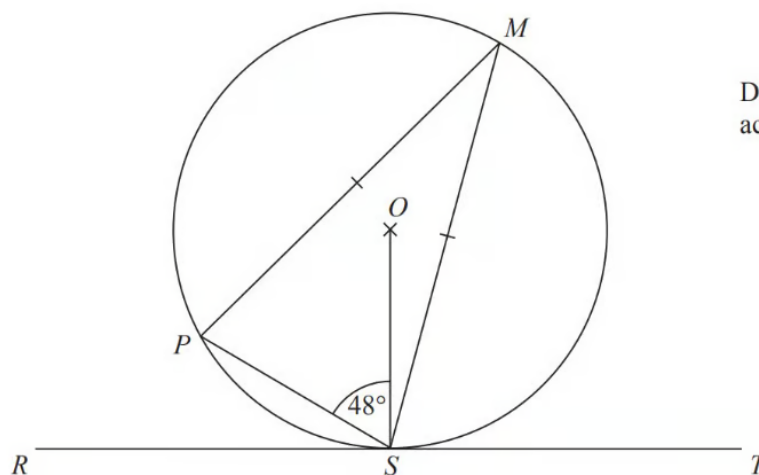


Diagram **NOT**
accurately drawn

P , M and S are points on a circle, centre O .
 RST is a tangent to the circle.

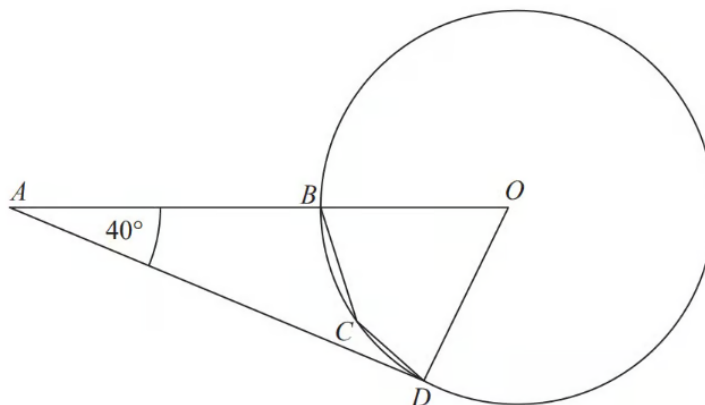
Angle $PSO = 48^\circ$
 $MP = MS$

Work out the size of angle MST .
Give reasons for each stage of your working.

(5 marks)

4

Diagram **NOT**
accurately drawn



B , C and D are points on the circumference of a circle, centre O . ABO is a straight line.

AD is the tangent at D to the circle.

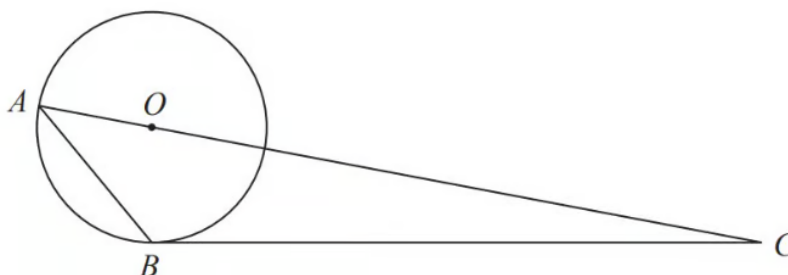
Angle $DAO = 40^\circ$

Work out the size of angle BCD .

Give a reason for each stage of your working.

(5 marks)

5



A and B are points on a circle, centre O .

BC is a tangent to the circle.

AOC is a straight line.

Angle $ABO = x^\circ$.

Find the size of angle ACB , in terms of x .

Give your answer in its simplest form.

Give reasons for each stage of your working.

(5 marks)

6

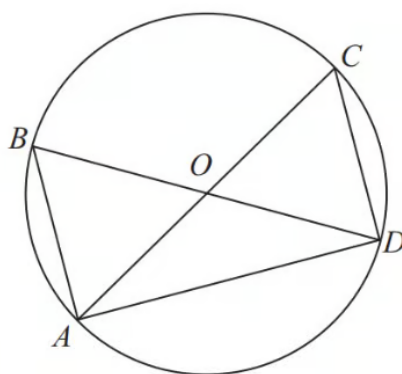


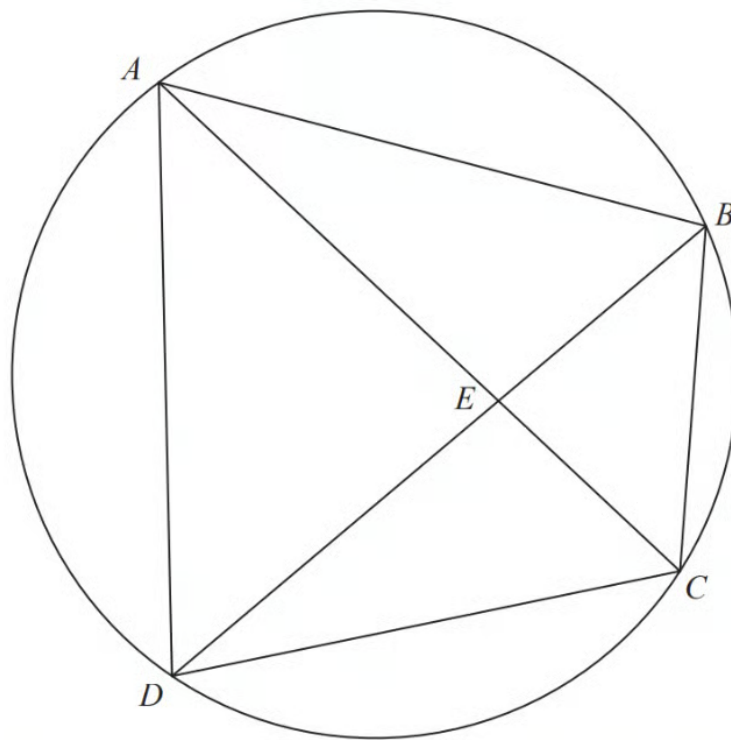
Diagram **NOT**
accurately drawn

AOC and BOD are diameters of a circle, centre O .

Prove that triangle ABD and triangle DCA are congruent.

(3 marks)

7 A , B , C and D are four points on the circumference of a circle.



AEC and BED are straight lines.

Prove that triangle ABE and triangle DCE are similar.

You must give reasons for each stage of your working.

(3 marks)

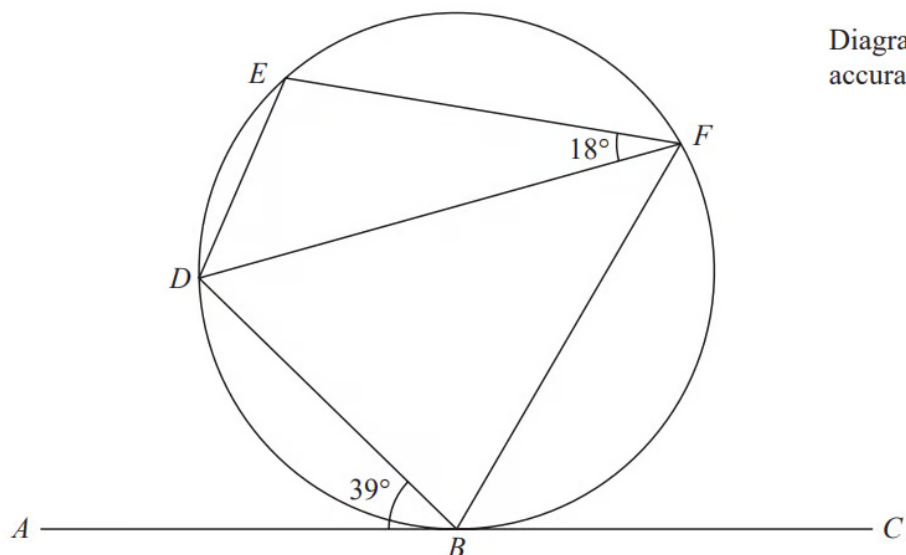


Diagram **NOT**
accurately drawn

B , D , E and F are points on a circle.

ABC is the tangent at B to the circle.

Angle $ABD = 39^\circ$

Angle $EFD = 18^\circ$

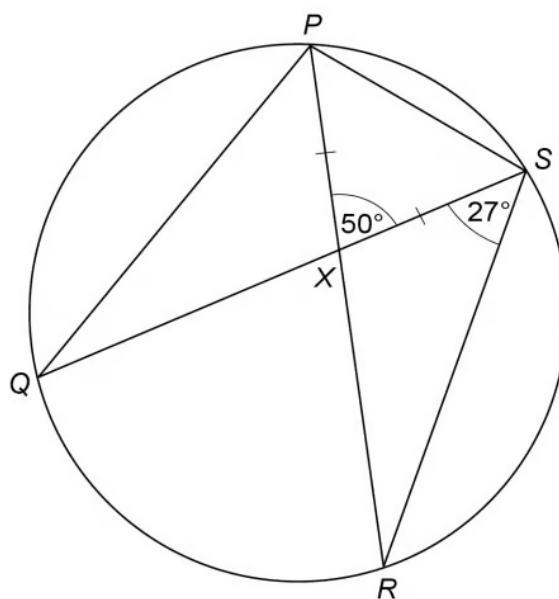
Work out the size of angle BDE .

Give reasons for your working.

(4 marks)

9 P , Q , R and S are points on a circle.

PXR and QXS are straight lines.
 $PX = SX$



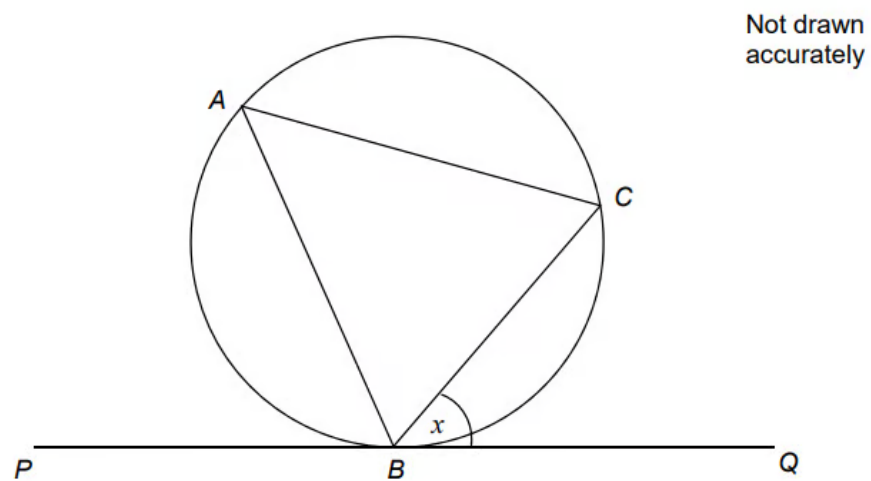
Not drawn
accurately

Prove that QS is **not** a diameter of the circle.

(4 marks)

10 A , B and C are points on a circle.

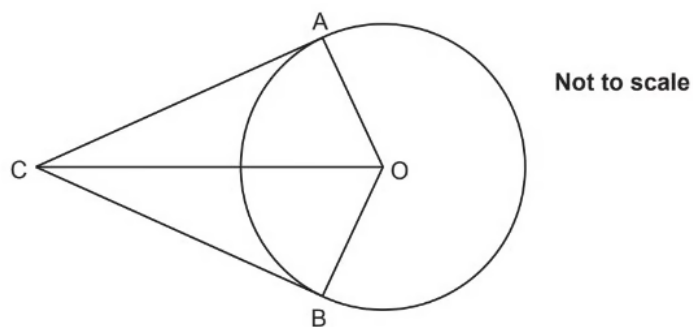
- BC bisects angle ABQ .
- PBQ is a tangent to the circle.



Angle $CBQ = x$
 Prove that $AC = BC$

(3 marks)

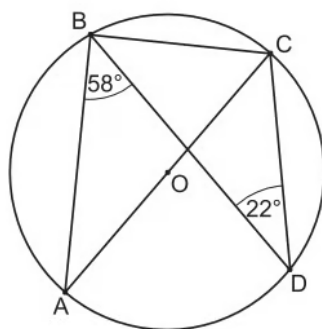
- 11 A and B are points on the circumference of a circle, centre O.
 CA and CB are tangents to the circle.



Prove that triangle OAC is congruent to triangle OBC .

(4 marks)

- 12 (a)** A, B, C and D are points on the circumference of a circle, centre O.
AC is a diameter of the circle.
Angle ABD = 58° .
Angle CDB = 22° .



Not to scale

Work out the sizes of angle ACD and ACB, giving reasons for your answers.

Angle ACD =°

(2 marks)

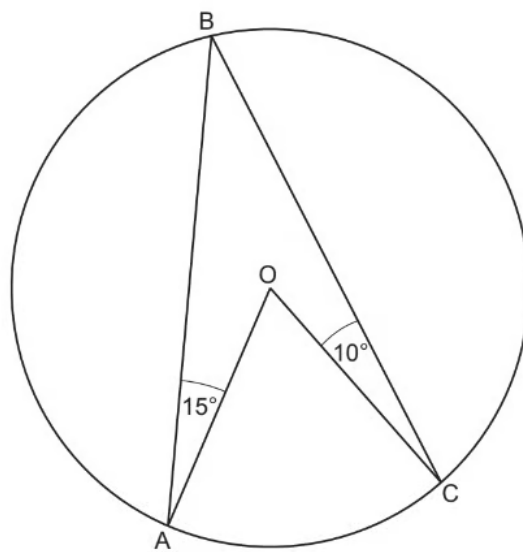
(b) Angle ACB =°

(3 marks)

13 In the diagram,

- A, B and C are points on the circumference of a circle
- O is the centre of the circle

- angle $OAB = 15^\circ$
- angle $BCO = 10^\circ$.



Not to scale

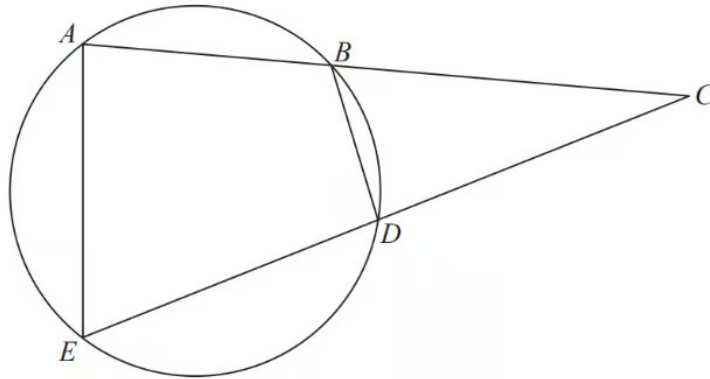
Calculate the acute angle AOC .

(4 marks)

Very Hard Questions

1

Diagram **NOT**
accurately drawn

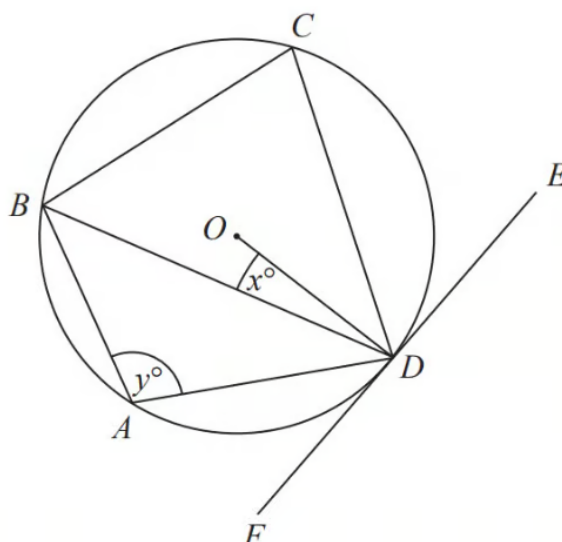


A , B , D and E are points on a circle.
 ABC and EDC are straight lines.

Prove that triangle BCD is similar to triangle ECA .
You must give reasons for your working.

(5 marks)

2 (a)



A , B , C and D are points on the circumference of a circle, centre O .
 FDE is a tangent to the circle.

Show that $y - x = 90$

You must give a reason for each stage of your working.

(3 marks)

(b) Dylan was asked to give some possible values for x and y .

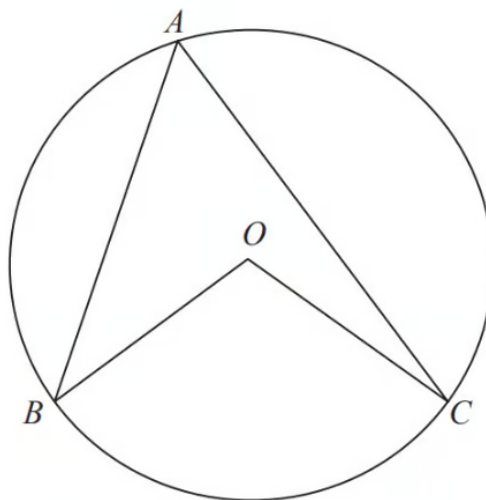
He said, " y could be 200 and x could be 110, because $200 - 110 = 90$ "

Is Dylan correct?

You must give a reason for your answer.

(1 mark)

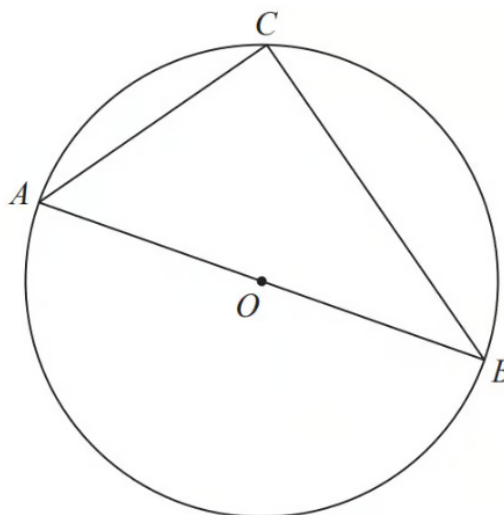
3 A , B and C are points on the circumference of a circle centre O .



Prove that angle BOC is twice the size of angle BAC .

(4 marks)

4



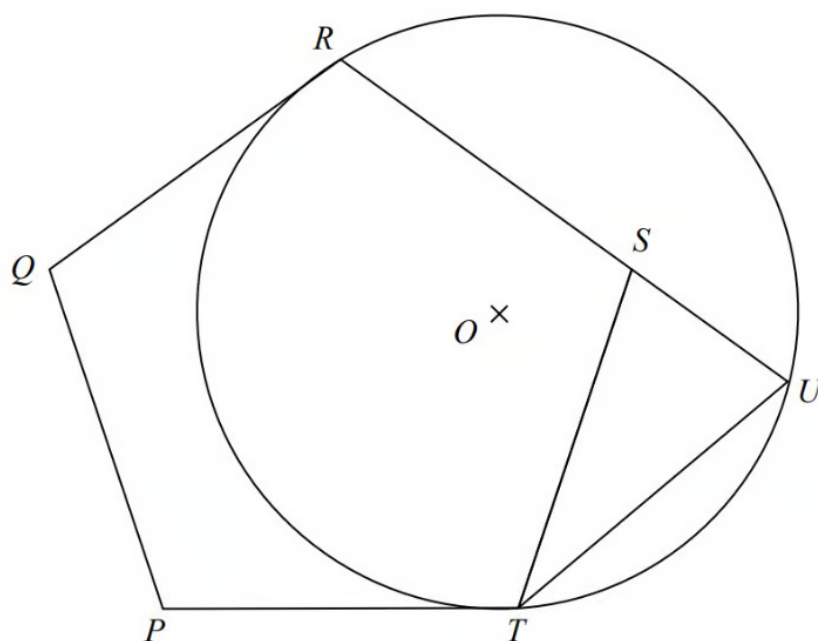
A , B and C are points on the circumference of a circle, centre O . AOB is a diameter of the circle.

Prove that angle ACB is 90°

You must **not** use any circle theorems in your proof.

(4 marks)

5

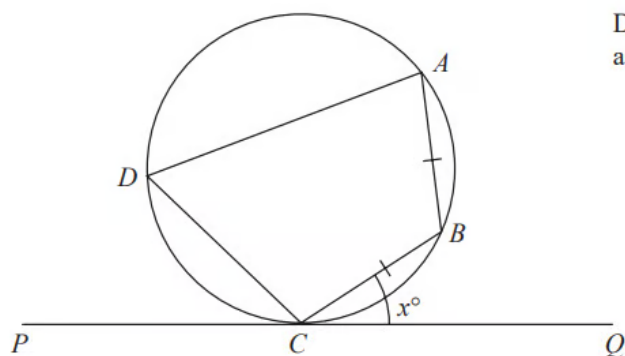


$PQRST$ is a regular pentagon.
 R , U and T are points on a circle, centre O .
 QR and PT are tangents to the circle.
 RSU is a straight line.

Prove that $ST = UT$.

(5 marks)

Diagram **NOT**
accurately drawn

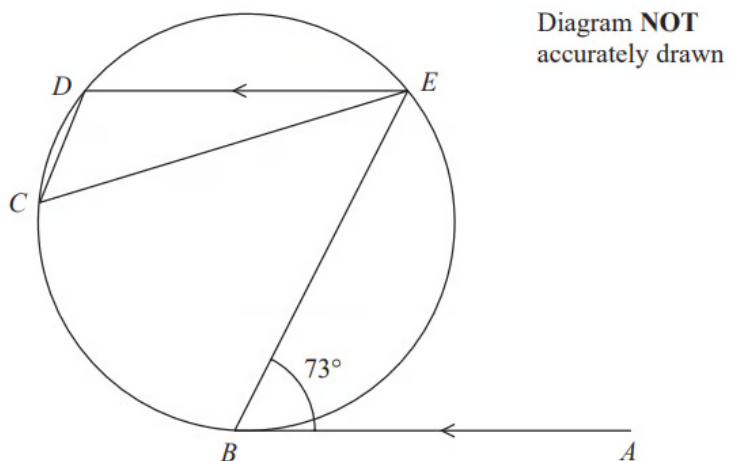


A , B , C and D are points on a circle.
 PCQ is a tangent to the circle. $AB = CB$.

Angle $BCQ = x^\circ$

Prove that angle $CDA = 2x^\circ$
 Give reasons for each stage in your working.

(5 marks)



B , C , D and E are points on a circle.

AB is the tangent at B to the circle.

AB is parallel to ED .

Angle $ABE = 73^\circ$

Work out the size of angle DCE .

Give a reason for each stage of your working.

(5 marks)

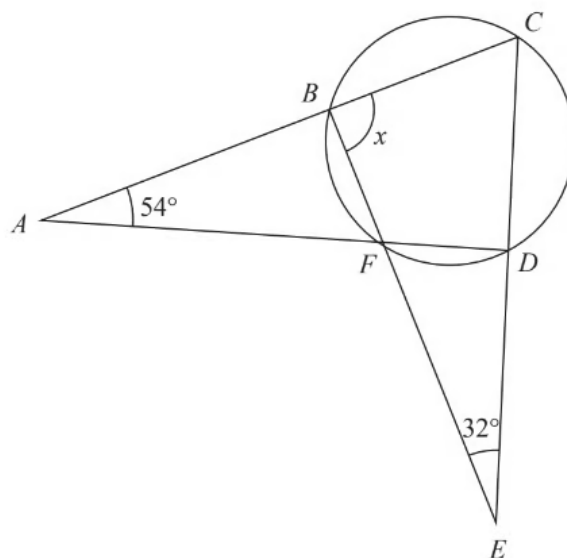


Diagram **NOT**
accurately drawn

B , C , D and F are points on a circle.
 ABC , AFD , BFE and CDE are straight lines.

Work out the size of angle x .
 Show your working clearly.

$x = \dots\dots\dots$

(4 marks)

- 9 A , B and C are points on a circle with centre O .

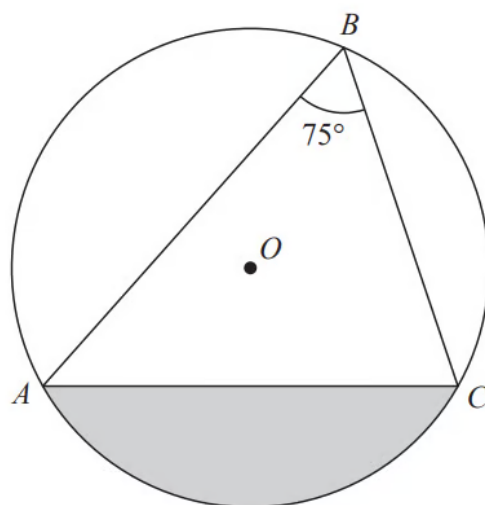


Diagram **NOT**
accurately drawn

Angle $ABC = 75^\circ$

The area of the shaded segment is 200cm^2

Calculate the radius of the circle.

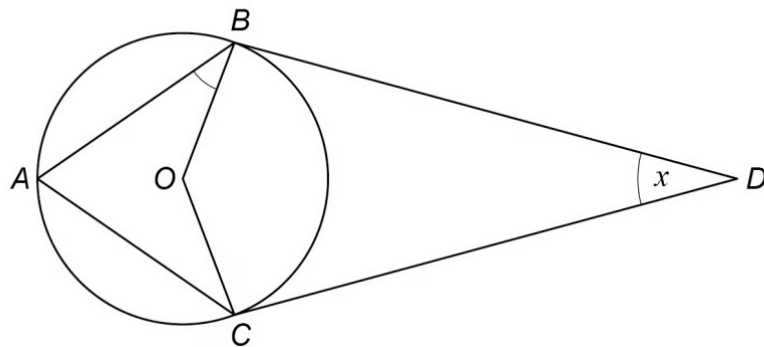
Give your answer correct to 3 significant figures.

..... cm

(5 marks)

- 10 A , B and C are three points on the circumference of a circle, centre O .

BD and CD are tangents to the circle.
 $ABDC$ is a kite.
 Angle BDC is x



Not drawn
accurately

Prove that angle ABO is $45^\circ - \frac{x}{4}$

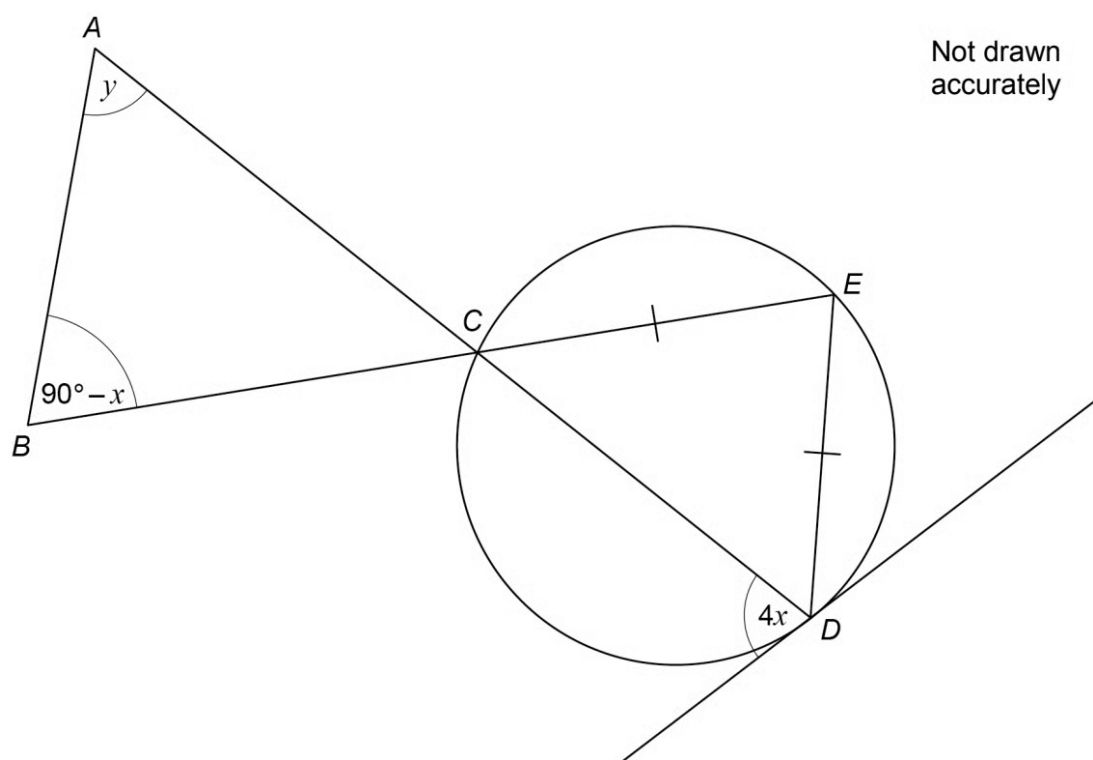
(4 marks)

11 C , D and E are points on a circle.

$$CE = DE$$

The tangent at D is shown.

ACD and BCE are straight lines.



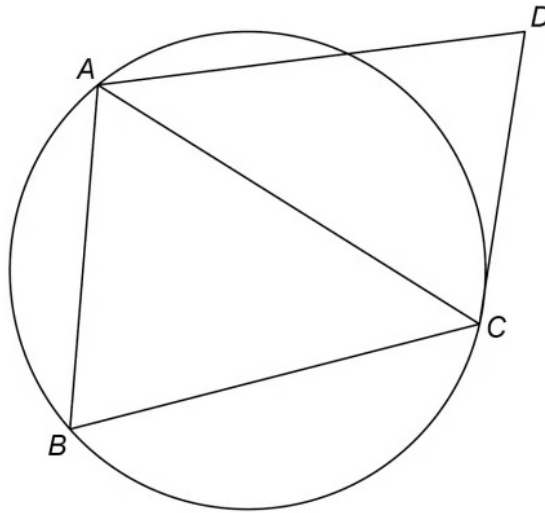
Prove that $y = 3x$

(4 marks)

12 (a) A , B and C are points on a circle.

CD is a tangent.

Not drawn
accurately



Assume that triangle ABC is isosceles with $AC = BC$

Prove that AB is parallel to DC .

(4 marks)

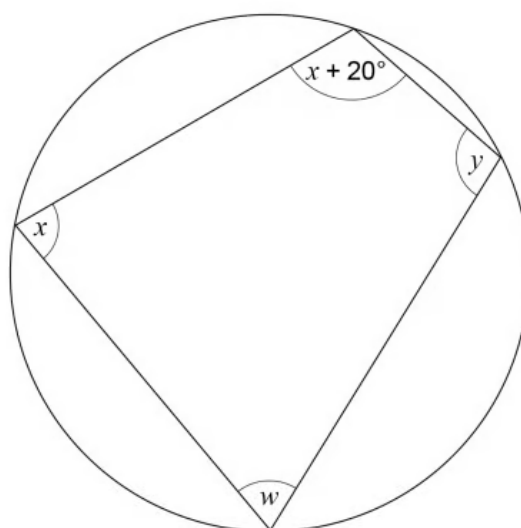
(b) In fact, triangle ABC is equilateral.

Tick the **two** boxes for the statements that **must** be correct.

☐	AB is parallel to DC
☐	AC bisects angle BCD
☐	AC bisects angle BAD

(1 mark)

13 Here is a cyclic quadrilateral.



Not drawn
accurately

$$x : y = 5 : 7$$

Work out the size of angle w .

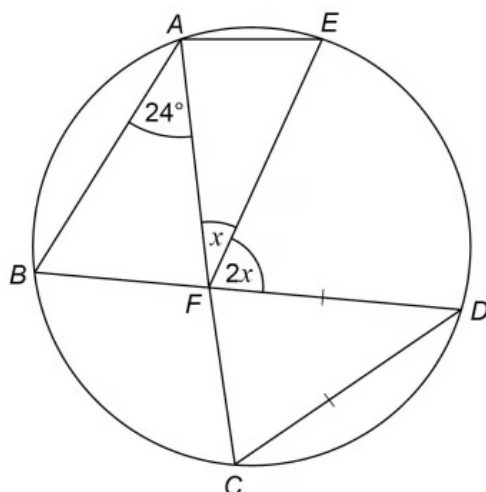
.....degrees

(4 marks)

14 A, B, C, D and E are points on a circle.

BFD and AFC are straight lines.

$$DC = DF$$



Not drawn
accurately

Work out the size of angle x .

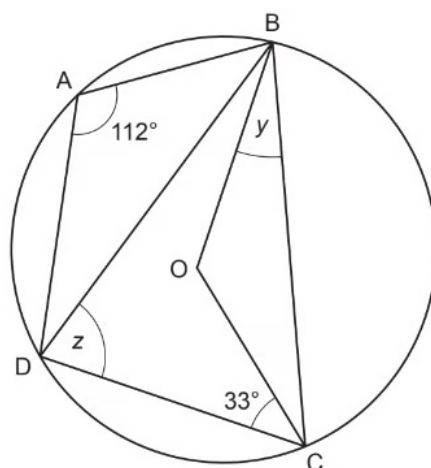
You **must** show your working which may be on the diagram.

.....degrees

(4 marks)

15 (a) A, B, C and D are points on the circumference of a circle, centre O .

Angle $BAD = 112^\circ$ and angle $DCO = 33^\circ$.



Not to scale

Show that angle $y = 35^\circ$.

Give reasons for each stage of your working.

(4 marks)

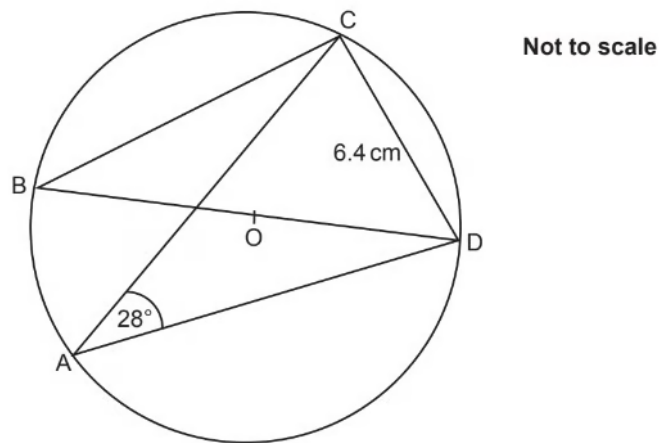
(b) Work out angle z .

Give reasons for your answer.

Angle $z = \dots\dots\dots^\circ$ because $\dots\dots\dots$

(3 marks)

- 16 A, B, C and D are points on the circumference of a circle, centre O.



Angle CAD = 28° and $CD = 6.4\text{cm}$.
BD is a diameter of the circle.

Calculate the area of the circle.

..... cm^2

(5 marks)